

# Lighting Difference based Wrinkle Mapping for Expression Synthesis

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**Abstract**—Nowadays, facial expression synthesis is widely used in expression simulation, recognition and animation. Texture feature (wrinkle) after face deformation largely reflects the genuineness of the synthesized expression, whose mapping is a critical step to the expression synthesis application. However, current lighting ratio based wrinkle mapping is sensitive to small source lighting and large lighting difference. In this work, a novel wrinkle mapping based on lighting difference fitting is proposed to improve the genuineness and robustness of mapped wrinkles. Experimental results on expression synthesis with large lighting difference show that the proposed algorithm is competitive on synthesizing visually genuine expressions.

## I. INTRODUCTION

With the development of face recognition and facial animation, expression synthesis has been increasingly important and widely used in these applications. Low-quality 2D images and 3D depth maps were mapped to realistic facial expressions by optimization with geometry and texture registration [1]. Features of 2D geometric deformation were employed for the facial expression recognition [2], where 2D deformable models tracking the greatest facial expression intensity were used for SVM classification. Other algorithms related with facial deformation and synthesis for expression recognition were also reported in [3], [4], [5]. Generally, the algorithms of expression synthesis are mainly divided into two categories, the 3D based and the 2D based.

The 3D based expression synthesis often requires a matching between 2D image and 3D shape or a database of basic expression set with respect to (w.r.t.) the target person, which is time consuming.

Unlike the 3D based expression synthesis, the 2D based algorithms learn geometry and texture features of the reference (source) expressions and map these features directly onto the target face. According to the type of the reference expressions, the 2D based algorithms are classified into two classes, one class is based on statistical learning of multiple reference expressions, the other is based on face deformation and wrinkle mapping which demands a single expression.

The statistically based algorithms generally require the following steps:

- Extract the corresponding feature points on faces of source neutral ( $F_{sn}$ ), source expression ( $F_{se}$ ) and target neutral ( $F_{tn}$ );

- Divide the face region into small parts and extract the regions containing expression features;
- Based on a source expression for simulating or a database of expressions w.r.t. the considered person, synthesize or simulate the new expression.

In the work of Beymer et al. [6], the synthesis of the expression was divided into phases of analysis and synthesis. The principle component analysis (PCA) was used to simulate new expressions by changing the coefficients of principle components corresponding to the expression feature points [7]. This method adopted facial region segmentation and interpolation to simulate the wrinkles on the face. However, it may not work when the size of the face is largely changed. Methods of bilinear kernel regression [8] and facial animation parameters (FAPs) [9] were also employed for the statistically modeling of the expression synthesis. For statistically based algorithms, a database of referred expressions w.r.t. the considered person is needed in general, and these methods mainly concentrate on the detail preservation of the generated expression.

The deformation and mapping based algorithms generally require the following steps:

- Location and alignment of the feature points on faces of  $F_{sn}$ ,  $F_{se}$  and  $F_{tn}$ ;
- Deformation of the target face  $F_{tn}$  by learning the movement from  $F_{sn}$  and  $F_{se}$ ;
- Wrinkle mapping on the deformed face of  $F_{tn}$ .

### A. Correspondence Matching and Face Deformation

For the aspect of face correspondence, Liu et al. [10] and Zhang et al. [11] located the positions and correspondence of the feature points manually. Song et al. [12] made this step semi-automatic. Actually, this step can be made more automatic by employing face alignment algorithms, such as the optical flow employed by Li et al. [13], the minimization optimization of an energy function proposed by Qian et al. [14] and Liao et al. [15] and cascade of regression trees adopted in [16], [17].

For 2D deformation algorithms, there were some interpolation based deformation [7], [8], while the obtained deformation shape is apt to lose some geometry features on the non-feature points. The wrapping algorithm in [18] obtained the weighted movement of each pixel, which was adopted in the expression synthesis algorithms [10], [12] for the face mesh

deformation. The feature points on the deformed target face were approximated with the weighted positions of the feature points by an elastic model [11]. A global optimization model for 2D shape deformation was presented in [19].

### B. Wrinkle Mapping

For the aspect of wrinkle mapping, unlike the 3D wrinkle generation [20], [21] by modeling wrinkles and deformation for the 3D expression synthesis, the 2D wrinkle simulation needs only learn and map the reference wrinkle features. Liu et al. [10] constructed a method for preserving the facial characteristics (e.g. the wrinkles), where the expression ratio image (ERI) between  $F_{sn}$  and  $F_{se}$  was assumed to be the same as that between  $F_{tn}$  and  $F_{te}$ . The expression features with ERI was mapped to the retrieved and deformed face sequence to obtain the final expression sequence [13]. Shift ERI incorporated with Gaussian damping weighting term was employed to map the wrinkles onto the target face [11]. These ratio based algorithms of lighting mapping are largely influenced by the abnormal lighting ratios when the lighting values of pixels on  $F_{sn}$  is relatively small. To avoid this disadvantage, we adopt the difference of the lightings [22] rather than the ratio between corresponding pixels on  $F_{sn}$  and  $F_{se}$  to simulate the lighting changes on the synthesized object. Moreover, a fitting form of the lighting difference is proposed.

In this work, a novel wrinkle mapping incorporating with mesh deformation (abbreviated as DaWF) is proposed to synthesize the facial expressions. The main contribution of the proposed DaWF concentrates on the ability of generating more genuine expressions in the stage of wrinkle mapping by solving a system of linear equations to fit lighting differences. Comparative results with several related algorithms in Section III-A reveal that the proposed mapping method can generate more complete wrinkle and is both robust and efficient.

This paper is structured as follows. Section II gives a description about the proposed algorithm step by step. The experimental results of the proposed algorithm on varieties of expressions are presented in Section III. Finally, discussions and some conclusions are addressed in Section IV.

## II. THE PROPOSED ALGORITHM

### A. Framework of the Algorithm

As presented in Fig. 1, the general framework of the proposed DaWF consists of three steps. In the first step, the correspondence feature points are located and slightly adjustment. In the second step, we obtain the deformed geometry by mesh deformation. The wrinkles are mapped onto the deformed face in the last step.

### B. Feature Location

As shown in Fig. 1(b), we view the whole face as a structure  $\Gamma = \{\Gamma_1, \dots, \Gamma_n\}$  which consists of eight parts i.e. two eyes, two brows, nose, mouse, lip and profile. For the feature location, active shape model (ASM) [23] is first employed to obtain the initial positions of these feature points including forehead region. Fig. 1(b) shows the location of the 79 feature

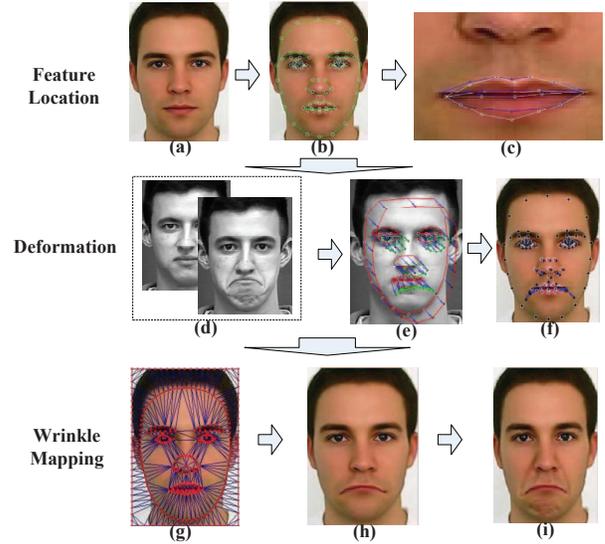


Fig. 1: The framework of the proposed algorithm.

points. However, the location is not accurate enough for the expression synthesis with large deformation. Thus, face part based active appearance model (AAM) [24] is employed to locate more accurate 68 feature points along part boundary edges, which are further used to trim the initial feature points on part boundary.

### C. Mesh Deformation

The procedure of generating the feature points on  $F_{te}$  is divided into three steps.

In the first step, point alignment is performed to avoid the influence of rotation. All the feature points are first rotated to an unified coordinate system with reference to the positions of the two eyes and the nose on the  $F_{sn}$  and  $F_{tn}$  faces.

In the second step, initial positions of feature points on  $F_{te}$  are obtained according to the movements of feature points on  $F_{sn}$  and  $F_{se}$ , as demonstrated in Fig. 1(d),(e).

Given the central point of each part ( $CP_{(i)}^{sn}$ ,  $CP_{(i)}^{tn}$ ), the widths ( $W_{sn}^{(i)}$ ,  $W_{tn}^{(i)}$ ) and the heights ( $H_{sn}^{(i)}$ ,  $H_{tn}^{(i)}$ ) in the unified coordinate framework of the faces  $F_{sn}$ ,  $F_{tn}$ , the positions of the feature points on  $F_{te}$  are estimated as follows:

$$V_{(i,j)}^{te} = CP_{(i)}^{tn} + (V_{(i,j)}^{se} - CP_{(i)}^{sn}) \begin{pmatrix} \frac{W_{tn}^{(i)}}{W_{sn}^{(i)}} \\ \frac{H_{tn}^{(i)}}{H_{sn}^{(i)}} \end{pmatrix}. \quad (1)$$

where  $V_{(i,j)}^{te}$  denotes the  $j$ -th feature points on the  $i$ -th part on the face  $F_{te}$ .

Finally, the algorithm of mesh deformation [11] with elastic model is employed to obtain the final deformation triangular mesh using the target feature points  $V_{(i,j)}^{te}$ . The initial triangular mesh of  $F_{tn}$  and the corresponding deformation face are presented in Figs. 1(g),(h), respectively, where the deformed face is further used for wrinkle mapping the following section.

#### D. Wrinkle Mapping Based on Lighting Difference Fitting

After the deformation of the parts, the texture details (such as the wrinkle) are needed to be mapped onto the target expression face. In the work [10], the wrinkle was reflected as the lighting variants at the pixel (the Y component of the YUV colors). They further proposed a pixel-by-pixel assignment form to simulate the lighting of the pixel on the face  $F_{te}$  in equation (2):

$$\mathcal{B}'(u, v) = \mathcal{B}(u, v)ERI_{u,v}, \text{ with } ERI_{u,v} = \frac{\mathcal{A}'(u, v)}{\mathcal{A}(u, v)}. \quad (2)$$

where  $\mathcal{A}(u, v)$ ,  $\mathcal{A}'(u, v)$  and  $\mathcal{B}(u, v)$  correspond to the lighting intensities of  $F_{sn}$ ,  $F_{se}$  and  $F_{tn}$ , respectively.

The formula in equation (2) is based on the ratio of the lightings, and each pixel on  $F_{te}$  learns the lighting change from only one corresponding pixel on  $F_{se}$ . In the following, a difference based lighting mapping is introduced and implemented by solving a system of linear equations, where each pixel learns from the lighting differences of the adjacent eight pixels and this method is robust from abnormal lighting ratios when the pixel lighting  $\mathcal{A}(u, v)$  is relatively small.

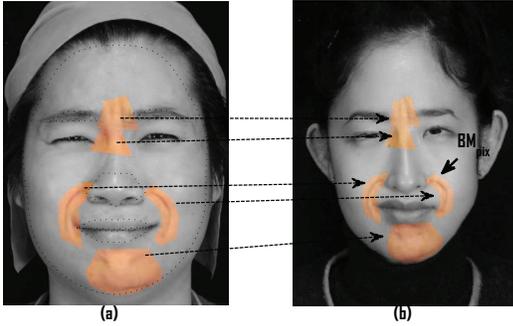


Fig. 2: The extraction and correspondence of wrinkle regions. (a): The extraction of wrinkle regions on  $F_{se}$  with colored label. (b): The corresponding wrinkle regions  $BM_{pix}$  on  $F_{te}$ .

First, the regions on the face  $F_{te}$  where the wrinkles need to be manually extracted and mapped, which are denoted as  $BM_{pix}$ . Fig. 2 demonstrates the extraction and mapping of wrinkle regions. The corresponding lightings of faces  $F_{sn}$ ,  $F_{se}$ ,  $F_{tn}$  in the  $3 \times 3$  adjacent region around the position  $(p, q)$  are denoted as  $\{l_{p,q}^{(sn)}, l_{p,q}^{(se)}, l_{p,q}^{(tn)}; i-1 \leq p \leq i+1, j-1 \leq q \leq j+1\}$ . Then the corresponding lightings on the face  $F_{te}$  are assumed to satisfy the constraints in equation (3)-(4).

For  $(i, j) \in BM_{pix}$

$$\begin{cases} (l_{p,q}^{(te)} - l_{i,j}^{(te)}) = (l_{p,q}^{(tn)} - l_{i,j}^{(tn)}) + \\ \lambda_r \cdot [(l_{p,q}^{(se)} - l_{i,j}^{(se)}) - (l_{p,q}^{(sn)} - l_{i,j}^{(sn)})], \end{cases} \quad (3)$$

$$i-1 \leq p \leq i+1, j-1 \leq q \leq j+1.$$

where  $\lambda_r = \frac{CE_{t,r}}{CE_{s,r}}$ ,  $CE_{s,r}$ ,  $CE_{t,r}$  are the changed extents of lightings of the  $r$ -th wrinkle region on  $F_{sn}$ ,  $F_{tn}$ , respectively, which are approximated by the difference of the 95% largest and 5% largest lightings of each region  $BM_{pix}$  to alleviate the influence of the abnormal lightings.

For  $(i, j) \notin BM_{pix}$

$$l_{i,j}^{(te)} = l_{i,j}^{(tn)}. \quad (4)$$

The equation (3) incorporating with equation (4) are then converted into one whole system of linear equations:

$$\begin{cases} A \cdot L|_{BM_{pix}} = B \\ L|_{\overline{BM_{pix}}} = L_0 \end{cases} \quad (5)$$

where  $L = \{l_{i,j}^{(te)}, (i, j) \in BM_{pix}\}$ ,  $A, B$  correspond to the coefficient matrixes constructed by equation (3),  $\overline{BM_{pix}} = \Omega - BM_{pix}$  and  $\Omega$  is entire facial region,  $L_0$  records the corresponding lightings on the face  $F_{tn}$ . The least squares of this system  $(A^T \cdot A) \cdot L = A^T \cdot B$  is then solved by the sparse LU decomposition.

Equation (5) is not well formulated when the lighting differences between  $F_{se}$  and  $F_{sn}$  along edges of wrinkle regions are significant, which makes the mapped wrinkles look not genuine enough on these edges. Thus, attenuation weight coefficient  $\lambda_r(d)$  is introduced to substitute for  $\lambda_r$  in equation (3), which is defined as follows:

$$\lambda_r(d) = \begin{cases} \lambda_r \cdot \sin(\frac{\pi}{2} \cdot \frac{d}{d_0}), & d \leq d_0 \\ \lambda_r, & d > d_0 \end{cases} \quad (6)$$

where  $d$  is the distance between the considered pixel in the wrinkle region and the nearest edge,  $d_0 = 5$  is a critical distance,  $\lambda_r$  is the  $r$ -th lighting ratio which is defined in equation (3).

### III. EXPERIMENTAL RESULTS

We perform the experiments on a PC with a 3.2GHZ core processor and 4 GB RAM. The set of all the expressions used in this test is shown in Fig. 3, where (a) shows an average man face downloaded from web, (b),(c) and the last row of expressions are neutral face images and the corresponding smile, sad and chuckle expression images used in paper [10] for testing. The expression of (d),(e) are faces of the 116-th person in the database [25].

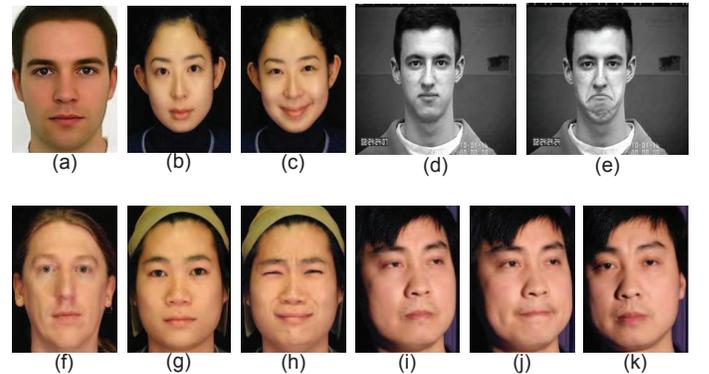


Fig. 3: The expression set used in the experimental test.

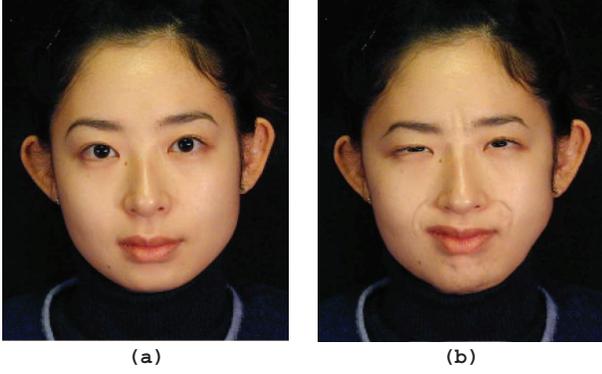


Fig. 4: (a),(b): The neutral and synthesized *sad1* expression of a little girl using Fig. 3(g) and (h) as  $F_{sn}$  and  $F_{se}$ .

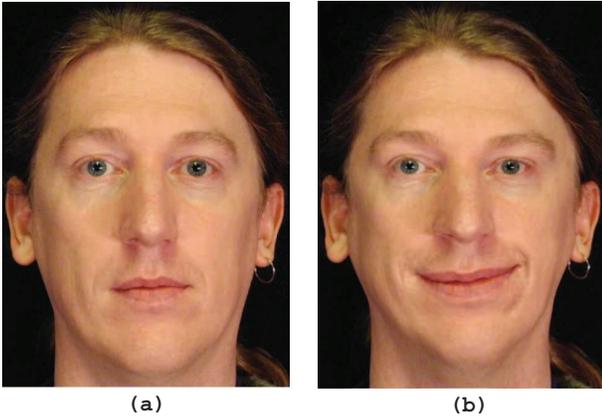


Fig. 5: (a),(b): The neutral and synthesized smile expression of a middle-aged man using Fig. 3(b) and (c) as  $F_{sn}$  and  $F_{se}$ .

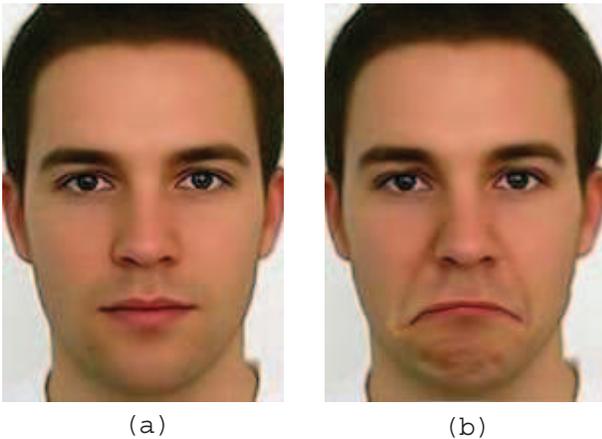


Fig. 6: (a),(b): The neutral and synthesized *sad2* expression of the average man using Fig. 3(d) and (e) as  $F_{sn}$  and  $F_{se}$ .

### A. Results of Wrinkle Mapping

To test the wrinkle mapping performance in overall, Figs. 4-6 present the results of sad (*sad1*), smile and sad (*sad2*) expressions mapped onto a little girl, a middle-aged man and an average man, when Figs. 3(g),(b),(d) are used as  $F_{sn}$  and Figs. 3(h),(c),(e) are used as  $F_{se}$ . The *sad1* expression in Fig. 3(h) implies the deformations of the face profile, eyes and the mouth, which generate wrinkles on the regions between two brows and eyes, the cheeks and the lower jaw. It can be seen from Fig. 4(a),(b) that the geometry shape and the wrinkles are synthesized properly. The wrinkles on left mouth tip of the smiling face of Fig. 3(c) are not obvious, the proposed DaWF preserves this detail in Fig. 5(b). The wrinkle texture on two face cheeks and chin region of *sad2* expression in Fig. 3(e) are complicated and chaotic, the proposed mapping form preserves these features genuinely in Fig. 6(b).

### B. Comparison with Related Algorithms

Three related algorithms, i.e. expression ration image (ERI) [10], vertex tent coordinate [12] and musical model (MD) [11] are chosen here for comparison.

1) *Metrics for Comparison*: To compare the performance quantitatively, a metric formulated in equation (7) is defined as the correlation of the lighting differences between the source and synthesized faces, which reflects the similarity of  $F_{se}$  and  $F_{te}$ .

$$CorD = \frac{\langle \nabla L_{src}, \nabla L_{syn} \rangle}{\|\nabla L_{src}\|_2 \cdot \|\nabla L_{syn}\|_2}. \quad (7)$$

where  $\langle \cdot, \cdot \rangle$  is the inner product of two vectors.

The overall runtime (*RT*) of expression synthesis is also considered in the comparison, where the time cost on extracting the wrinkle regions is not included, as all the considered algorithms need to manually determine the locations of wrinkle regions. For the programming implementation, hybrid of MATLAB and C++ is employed to make use of the advantage of MATLAB software at the matrix computation and the efficiency of C++ at loop iteration. The smoothing operator and lighting mapping in ERI, the lighting mapping with shift ERI in MD algorithm and the procedures of constructing coefficient matrices in VTC and DaWF are coded in C++ to accelerate the implementation.

2) *Visual Inspection*: Fig. 7 presents the comparative results of our algorithm with several related algorithms on *sad1* expression synthesis using Fig. 3(g),(h) and (b) as  $F_{sn}$ ,  $F_{se}$  and  $F_{tn}$ , respectively. In this experimental test, the mesh deformation in the algorithm MD [11] was used for all competing approaches.

From the aspect of visual performance, it is demonstrated in Figs. 7(a)-(e) that the proposed DaWF preserves more complete wrinkles than the other algorithms on the cheek region. To demonstrate the detailed information of these algorithms on lighting preservation, Fig. 7(f)-(j) present lighting differences between the source and synthesized expressions on the region between two eyes, two cheeks and the lower jaw by different algorithms. One can observe from Figs. 7(g)-(j)

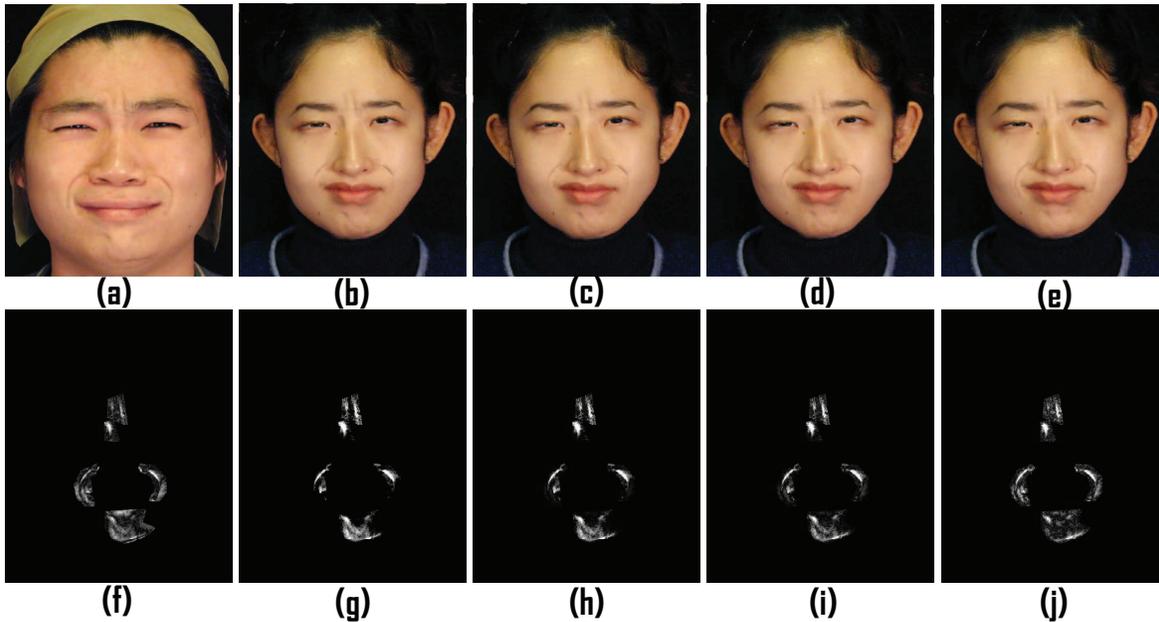


Fig. 7: The comparison of four algorithms on wrinkle mapping. (a) is the source sad expression, (b)-(e) are synthesized sad expressions obtained by the algorithm ERI [10], VTC [12], MD [11] and the proposed DaWF, respectively. (f) reflects the lighting difference between  $F_{sn}$  and  $F_{se}$  on four key wrinkle regions, (g)-(j) demonstrate the lighting differences between  $F_{tn}$  and  $F_{te}$  by the algorithms ERI, VTC, MD, DaWF, respectively.

TABLE I: Comparative results of the proposed algorithm and other algorithms in literature.

Algorithm	$RT(s)$ ( <i>sad1</i> , Smile, <i>sad2</i> )	$CorD$ ( <i>sad1</i> , Smile, <i>sad2</i> )	Preprocessing Needed	Lighting Mapping	Additional Parameters
ERI [10]	(8.4, 2.4, 1.0)	(0.74, 0.76, 0.69)	Smoothness filtering	ERI	$c$
VTC [12]	(12.3, 2.1, <b>0.8</b> )	(0.83, <b>0.82</b> , 0.73)	Correspondence modification	Covariance of ratios	-
MD [11]	( <b>7.9</b> , 2.5, 0.9)	(0.81, 0.82, 0.72)	A database of expressions	Shift ERI	$h(u_0, v_0), \lambda_k, w_{ab}, r(u_0, v_0)$
DaWF	(9.6, <b>2.0</b> , 0.8)	( <b>0.87</b> , 0.79, <b>0.75</b> )	Correspondence modification	Lighting difference	$\lambda_1-\lambda_3$

that the wrinkle difference obtained by the proposed DaWF is more similar to that of Fig. 7(f) than the other algorithms.

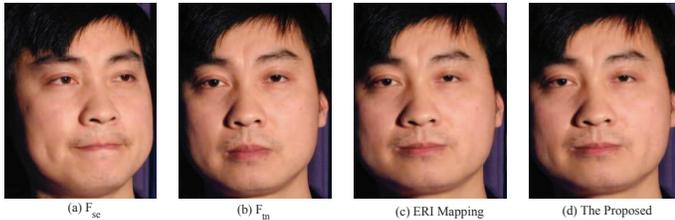


Fig. 8: The comparison of ERI and the proposed mappings for a non-frontal expression synthesis.

In the paper [10], Figs. 3(i),(j),(k) with non-obvious dimple wrinkles were used to test the algorithm performance on synthesizing frontal expression learning from non-frontal wrinkle features, where ERI format was reported to lose efficiency. In this work, we use Figs. 3(i),(j),(k) as  $F_{sn}$ ,  $F_{se}$  and  $F_{tn}$  for the testing. It can be seen from Fig. 8(d) that the proposed wrinkle mapping still achieves distinct wrinkle features on the left cheek, which further illustrates that the proposed mapping outperforms ERI mapping on preserving non-obvious expression features.

Tab. I lists the comparative results of these algorithms in terms of  $RT$  and  $CorD$  on *sad1*, smile, and *sad2* expression synthesis using Figs. 3(g),(b),(d) as  $F_{sn}$ , Figs. 3(h),(c),(e) as  $F_{se}$ , and Figs. 3(b),(f),(a) as  $F_{tn}$ . The image sizes for the expressions of *sad1*, smile and *sad2* are  $746 \times 621$ ,  $633 \times 469$  and  $207 \times 146$ , respectively.

Considering the overall runtime of expression synthesis, fitting-based algorithms VTC and DaWF outperform ERI based algorithms when the image size is small because the overall smoothness operation is not needed, which can be seen from  $RT$  values of smile expression synthesis in Tab. I.

Considering the metric of similarity, the difference form of the lighting adopted in the proposed DaWF achieves comparable results with the other algorithms. The proposed DaWF attempts to preserve the difference of lightings which is insensitive to abnormal lighting ratios, it is more robust and can map subtle lighting differences when the lighting  $l_{i,j}^{sn}$  on  $F_{sn}$  is small. One can observe from  $CorD$  values in Tab. I that DaWF achieves relatively better performance than the other algorithms.

#### IV. DISCUSSION AND CONCLUSION

In this work, an algorithm of expression synthesis (DaWF) with a novel strategy of wrinkle mapping is proposed, which is based on the fitting of lighting differences. Experimental results on various kinds of expressions and comparison with state-of-the-art algorithms illustrate the effectiveness and robustness of the wrinkle mapping method on detail preservation.

Although visually genuine expressions are synthesized by the proposed algorithm, there are still much margin for further improvements. Firstly, expression wrinkles need be detected automatically or semi-automatically to make it ease to use. Secondly, the algorithm of view morphing in [26] or 3D reconstruction algorithm in [27] can be integrated to synthesize expressions for largely rotated face in 3D space. Lastly, more efficient algorithm of mesh deformation should be devised to apply the proposed algorithm on expressions with large geometry deformation.

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